

Section 5.2: Synthetic division

#1- 10:

a) Perform the division using synthetic division.

b) if the remainder is 0 use the result to completely factor (the dividend is the numerator or the polynomial to the left of the division sign.)

1) $\frac{3x^3 - 17x^2 + 15x - 25}{x - 5}$

1a)
$$\begin{array}{r|rrrr} 5 & 3 & -17 & 15 & -25 \\ & \downarrow & 15 & -10 & 25 \\ \hline & 3 & -2 & 5 & 0 \end{array}$$

$$\frac{3x^3 - 17x^2 + 15x - 25}{x - 5} = 3x^2 - 2x + 5 \quad (R=0)$$

1b) $3x^3 - 17x^2 + 15x - 25 = (x - 5)(3x^2 - 2x + 5)$

($3x^2 - 2x + 5$ is prime)

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3) $\frac{4x^3+8x^2-9x-18}{x+2}$

3a)
$$\begin{array}{r|rrrr} -2 & 4 & 8 & -9 & -18 \\ & & -8 & 0 & 18 \\ \hline & 4 & 0 & -9 & 0 \end{array}$$

$$\boxed{\frac{4x^3+8x^2-9x-18}{x+2} = 4x^2-9 \quad (R=0)}$$

3b) $4x^3+8x^2-9x-18 = (x+2)(4x^2-9)$

$$\boxed{= (x+2)(2x+3)(2x-3)}$$

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5) $\frac{3x^3 - 16x^2 - 72}{x - 6}$

5a)

↓ 0x

$$\begin{array}{r|rrrr} 6 & 3 & -16 & 0 & -72 \\ & & 18 & 12 & 72 \\ \hline & 3 & 2 & 12 & 0 \end{array}$$

$$\frac{3x^3 - 16x^2 - 72}{x - 6} = 3x^2 + 2x + 12 \quad (R=0)$$

5b) $3x^3 - 16x^2 - 72 = (x - 6)(3x^2 + 2x + 12)$

↑
This is
PRIME

#1- 10:

a) Perform the division using synthetic division.

b) if the remainder is 0 use the result to completely factor the dividend (the dividend is the numerator or the polynomial to the left of the division sign.)

7) $(5x^3 + 6x + 8) \div (x + 2)$

7a)
$$\begin{array}{r|rrrr} -2 & 5 & 0 & 6 & 8 \\ & & -10 & 20 & -52 \\ \hline & 5 & -10 & 26 & -44 \end{array}$$

$$\frac{5x^3 + 6x + 8}{x + 2} = 5x^2 - 10x + 26 \quad R = -44$$

$$\text{OR } 5x^2 - 10x + 26 - \frac{44}{x + 2}$$

7b) Skip PART b
Since Remainder NOT 0

#1- 10:

a) Perform the division using synthetic division.

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9) $(x^3 - 27) \div (x - 3)$

Qa

$$\begin{array}{r|rrrr} 3 & 1 & 0 & 0 & -27 \\ & \downarrow & 3 & 9 & 27 \\ \hline & 1 & 3 & 9 & 0 \end{array}$$

$$(x^3 - 27) \div (x - 3) = x^2 + 3x + 9$$

9b) $x^3 - 27 = (x - 3)(x^2 + 3x + 9)$

↑
PRIME

#11 – 20:

a) use your graphing calculator, or the rational root theorem to find a x-intercept of the polynomial

b) use synthetic division to completely factor the polynomial

c) Use your answer to part a to solve $f(x) = 0$

11) $f(x) = x^3 + 2x^2 - 5x - 6$

11a)

$$x = -3 \text{ or } 2 \text{ or } -1$$

11b)

$$\begin{array}{r|rrrr} -3 & 1 & 2 & -5 & -6 \\ & & -3 & 3 & 6 \\ \hline & 1 & -1 & -2 & 0 \end{array}$$

$$x^3 + 2x^2 - 5x - 6 = (x+3)(x^2 - x - 2)$$
$$= (x+3)(x+1)(x-2)$$

11c) $f(x) = 0$

$$(x+3)(x+1)(x-2) = 0$$

$$x+3=0 \quad x+1=0 \quad x-2=0$$

$$x = -3 \quad x = -1 \quad x = 2$$

$$x = -3, -1, 2$$

#11 - 20:

a) use your graphing calculator, or the rational root theorem to find a x-intercept of the polynomial

b) use synthetic division to completely factor the polynomial

c) Use your answer to part a to solve $f(x) = 0$

13) $f(x) = 2x^3 - 13x^2 + 24x - 9$

13a) $x = 3$

13b)

$$\begin{array}{r|rrrr} 3 & 2 & -13 & 24 & -9 \\ & & 6 & -21 & 9 \\ \hline & 2 & -7 & 3 & 0 \end{array}$$

$$2x^3 - 13x^2 + 24x - 9 = (x-3)(2x^2 - 7x + 3)$$

factor $2x^2 - 7x + 3$

$$= (x-3)(2x-1)(x-3)$$
$$= (2x^2 - 6x)(-1x + 3) = \boxed{(x-3)^2(2x-1)}$$
$$= 2x(x-3) - 1(x-3)$$
$$= (x-3)(2x-1)$$

13c) $f(x) = 0$

$$(x-3)^2(2x-1) = 0$$

$$(x-3)(x-3)(2x-1) = 0$$

$$x-3=0 \quad x-3=0 \quad 2x-1=0$$

$$x=3 \quad x=3 \quad 2x=1$$
$$x=\frac{1}{2}$$

$$\boxed{x=3, \frac{1}{2}}$$

#11 - 20:

a) use your graphing calculator, or the rational root theorem to find a x-intercept of the polynomial

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c) Use your answer to part a to solve $f(x) = 0$

15) $f(x) = 6x^3 - 29x^2 - 62x + 120$

15a) $x = 6$

15b)
$$\begin{array}{r|rrrr} 6 & 6 & -29 & -62 & 120 \\ & & 36 & 42 & -120 \\ \hline & 6 & 7 & -20 & 0 \end{array}$$

$$6x^3 - 29x^2 - 62x + 120 = (x-6)(6x^2 + 7x - 20)$$

$$= (x-6)(3x-4)(2x+5)$$

factor $6x^2 + 7x - 20$

$$= (6x^2 - 8x) + (15x - 20)$$

$$= 2x(3x-4) + 3(3x-4)$$

$$= (3x-4)(2x+3)$$

15c) $f(x) = 0$

$$(x-6)(3x-4)(2x+5) = 0$$

$$\begin{aligned} x-6 &= 0 \\ x &= 6 \end{aligned}$$

$$\begin{aligned} 3x-4 &= 0 \\ 3x &= 4 \\ x &= \frac{4}{3} \end{aligned}$$

$$\begin{aligned} 2x+5 &= 0 \\ 2x &= -5 \\ x &= -\frac{5}{2} \end{aligned}$$

$$\sqrt{x=6, \frac{4}{3}, -\frac{5}{2}}$$

#11 – 20:

a) use your graphing calculator, or the rational root theorem to find a x-intercept of the polynomial

b) use synthetic division to completely factor the polynomial

c) Use your answer to part a to solve $f(x) = 0$

17) $f(x) = x^3 - 3x^2 + 4x - 12$

17a) $x = 3$

17b)
$$\begin{array}{r|rrrr} 3 & 1 & -3 & 4 & -12 \\ & & 3 & 0 & 12 \\ \hline & 1 & 0 & 4 & 0 \end{array}$$

$$x^3 - 3x^2 + 4x - 12 = (x - 3)(x^2 + 4)$$

↑
Prime

17c) $(x - 3)(x^2 + 4) = 0$

$$\begin{aligned} x - 3 &= 0 \\ x &= 3 \end{aligned}$$

$$\begin{aligned} x^2 + 4 &= 0 \\ x^2 &= -4 \\ x &= \pm 2i \end{aligned}$$

$$\boxed{x = 3, \pm 2i}$$

#11 – 20:

a) use your graphing calculator, or the rational root theorem to find a x-intercept of the polynomial

b) use synthetic division to completely factor the polynomial

c) Use your answer to part a to solve $f(x) = 0$

19) $f(x) = x^3 + 4x^2 + 25x + 100$

19a) $x = -4$

19b)
$$\begin{array}{r|rrrr} -4 & 1 & 4 & 25 & 100 \\ & & -4 & 0 & -100 \\ \hline & 1 & 0 & 25 & 0 \end{array}$$

$$x^3 + 4x^2 + 25x + 100 = (x+4)(x^2+25)$$

↑
Prime

19c) $f(x) = 0$

$$(x+4)(x^2+25) = 0$$

$$x+4=0$$

$$x = -4$$

$$x^2+25=0$$

$$\sqrt{x^2 = \pm 25}$$

$$x = \pm 5i$$

$$\boxed{x = -4, \pm 5i}$$